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[The Category of Glue_part-2](#)

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Abstract

See also part_1 – [here](#).

How to get rid of glue? From gluing to jumping. A new abstraction, the *as-abstraction*, and a subversion, the morpho-abstraction, has to be risked to avoid the complicity of category theory with the unavoidable exploitation of (conceptual) resources by the Western approach to interaction and communication in computer science. To overcome the limitations of the category "glue", contextualization and mediation in a chiasmic and diamond framework has to be elaborated and achieved to create chances to surpass and subvert such cultural and technological limitations.

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| K07 Contextual Programming Paradigm | |

Category of Glue, Part II

Is there any glue to stop the decline of Western culture?

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Abstract

Part I:

A typology of different categories of glue (ordinary, super-, para-, proto-, trans-glue) are glued together with different strategies of gluing (set and category theory, combining logics, bi-category with (co)spans, polycontextuality and diamond theory). Interpretations of “interactional glue”, “nerve glue”, “logical glue” are sketched. Keywords of the dissemination of the concept of “glue” in history (Hegel, Marx, Lenin, Gunther, Derrida, Obama) and strategies (Glue, Opium, Mediation) of gluing them together under a general parapluie (ontology, society, solidarity, fear) are critically sketched.

The economical question is: *Can we still afford to glue interactions together?*

The category of glue isn't blue. Categories are clueless to interaction and are banking unsecured resources.

Part II:

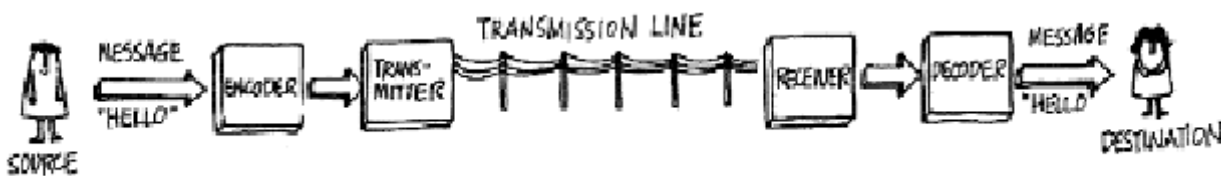
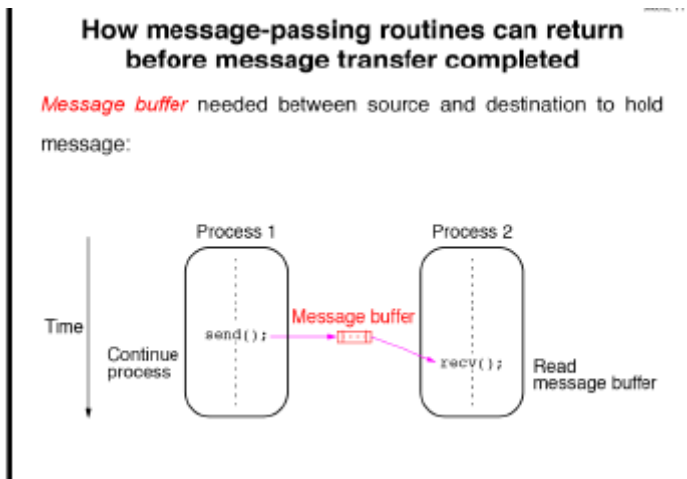
How to get rid of glue? From gluing to jumping. A new abstraction, the *as-abstraction*, and a subversion, the morpho-abstraction, has to be risked to avoid the complicity of category theory with the unavoidable exploitation of (conceptual) resources by the Western approach to interaction and communication in computer science.

To overcome the limitations of the category “glue”, contextualization and mediation in a chiasmic and diamond framework has to be elaborated and achieved to create chances to surpass and subvert such cultural and technological limitations.

1. Diamond theory of interactivity

1.1. Buffering super glue

1.1.1. Gluing information



"Whatever its nature (radio waves, wires, laser beams), the carrier is called a *transmission line* or wave. At the other end of this line the *message* is decoded and transcribed into *information* that has *meaning* for the person to whom it is addressed. But in order for the recipient to recognize and use the information, there must already have

been information *memorized* that can be compared with the message just received. A final and important point is that *disturbances* occurring in the transmission line (the "noise") can alter the message and change its meaning.” (de Rosnay)

Joël de Rosnay, THE MACROSCOPE, A NEW WORLD SCIENTIFIC SYSTEM

<http://pcp.vub.ac.be/macroscope/chap4.html>

1.1.2. Circularity of buffering information

There is obviously a kind of a well known circularity involved with the buffer paradigm.

A sender is sending a message to a receiver, but this procedure is not working directly from sender to receiver, but indirectly via a buffer. Hence, the buffer is a receiver too, albeit a semi-receiver, but in its functionality to act as a buffer it has to receive the message which has to be buffered. Therefore, the buffer to work as a receiver needs a buffer, his own semi-buffer, which is enabling the main buffer to buffer the message for a receiver. Again, this is only the beginning of an infinite regress. Our semi-buffer needs a semi-semi-buffer to semi-buffer the buffer to buffer the message for a receiver. And so on!

In other words: Super Glue isn't enough. What is needed is the *ultimate* super glue, the super glue of the super glue.

Some Hello!

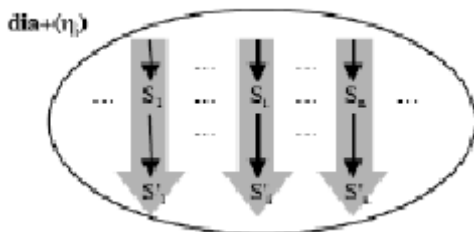
"Those links may make you pull your hair out! The "Glue" article is all over the place, but, I think, working around the problem you're addressing." (John Powers)

The style of this "Glue"-text might succeed to reflect, "all over the place" (John Powers), the lack of strict and save interconnections between its heterogeneous parts. Also, as much is still glued together by the metaphor "glue", the lack of continuity, deductive or explicative, is marking the *gaps* and the chances or challenges to choreograph jumps and salti to "bridge" together that what doesn't belong together. What belongs together, and might be glued for ever, like mankind, nation, family, identity, doesn't need to be bridged. It remains well placed and accessible in the labyrinth of the human cage.

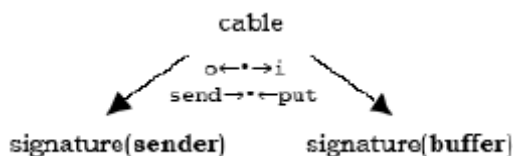
especially:

1.2. Streching super glue

1.2.1. Horizontally: Meta-pattern



"For instance, a configuration in which the messages from a sender component are sent (to a receiver) through a bounded buffer defines the following diagram:

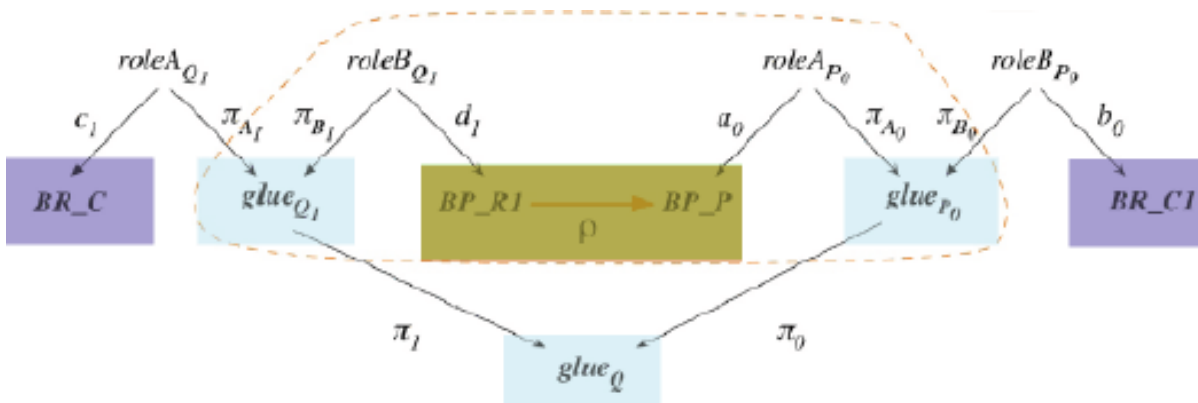


The node labelled *cable* is the representation of the set of bindings.” (Cat, p. 146)

<http://www.cs.le.ac.uk/people/jfiadeiro/>



Glue in action (Fiadeiro, p. 19, 2008)



1.2.2. Pfalzgraf's Fibered Glue

Another strategy of stretching and distributing glue is given by the general techniques of fibering and indexing categories. Where is the glue of fibered distribution, e.g. of agents in Multi-Agent Systems (MAS)?

Despite a great clarification of meta-glued fusions and confusions, meta-glue is still at work and necessary to enable interaction between distributed agents in the fibered polycontextural model of MAS. Fibered distribution is modeled in the framework of *bundle* categories along a general *index* fiber, i.e a “*base manifold*” (Pfalzgraf). The index fiber is gluing all those distributed free fibers together. Hence, fibered distribution is based on glue. This glue is gluing together all the fibers of stretched glue-fibres. The proposed techniques are highly sophisticated: the super glue is meta-gluing itself infinitely. That is, the base manifold or index set might be fibered itself. The construction is “recursive, fractal and self-referential” (Pfalzgraf), hence bottom-less.

<http://www.cosy.sbg.ac.at/~jpfalz/ACCAT-Tutorial-KI2004.html>

"Actually, when listening to the experts speaking about *polycontextural* logics, he was reminded of the concept of *fiber spaces*.

This led him to the idea of introducing “*logical fiberings*”, i. e. taking the abstract concept of fiber bundles and combine it with logical spaces as fibers all put together over a *base manifold* (which acts as *index set* with a particular structure). Thus over each point of the base space there sits (‘resides’) a fiber which can be interpreted as the *local state space* of that point (‘agent’).

The fiberings method is found to be very useful in modeling communication and interaction between cooperating agents, due to the possibility to switch between a *local/global* point of view which is inherent to this framework." Pfalzgraf et al, Towards a General Approach for Modeling Actions and Change in Cooperating Agents Scenarios, 1996

PFALZGRAF et al. Logic Jnl IGPL.1996; 4: 445-472

, <http://jigpal.oxfordjournals.org/cgi/content/abstract/4/3/445>

A more generalized approach to fibred logics is given recently by Pfalzgraf/Soboll as a “*base diagram*”, which is introduced with: “Fundamental important for our work is the observation that the general *communication* and *cooperation* structure of a MAS can be represented by a corresponding arrow diagram, called *base diagram* of the MAS.”

“To each MAS we associate such a *base diagram*, which represents the complete relational structure (i.e. communication in the general sense). The nodes of this arrow diagram represent *agents*, the arrows (and paths of arrows) hold the *communication* and *cooperation* information. This gives a category by its own right, more precisely a typed category.

In a MAS communication and cooperation (in general relations) between agents can change. This fact gives rise to the definition of the category **MAS** of all MAS where the objects are *base diagrams* of Multiagent Systems and the morphisms are **MAS** morphisms i.e. structure preserving maps between base diagrams.

Based on this category **MAS** a transformation system for Multiagent Systems can be established by applying the double pushout approach to Multiagent Systems.

[C]hecking the so called “*gluing condition*” solves this problem, in this paper we introduce an alternative algorithm.”

[cf. DPO: Double Push Out!]

Thomas Soboll, On the Construction of Transformation Steps in the Category of Multiagent Systems

<http://www.portal.acm.org/citation.cfm?id=1428606>

“The scenarios of cooperating robot agents were originally devised to demonstrate how the concept of a Logical Fibering can be used in a natural way to assign a system of Distributed Logics to a MAS, where every agent has an individual local logical state

space (fiber), the collection of all the fibers forms the global state space (fiber bundle) of the MAS.

This Fiber Bundle aspect can naturally be extended and generalized to introduce fibers of various structure types, modeling corresponding state space properties which are of relevance to model the complete state space of an agent, consisting of various modules (fibers) defining the complete type of an agent.” (Pfalzgraf, p.34)

1.2.3. What are the aims of glued interactions?

Service-oriented approach

“Services add a *social* layer of abstraction over a component infrastructure in sense that they structure the process of interconnection (*programmed interconnections*).

- Services should be published at a level of abstraction that corresponds to a real-world activity or recognisable business function (which is where social complexity can be understood)

- Systems should be *socially-reflective*.”

(Fiadeiro, 2008, p. 4)

Semantics of Service Discovery and Binding,

<http://www-lipn.univ-paris13.fr/~choppy/IFIP/URBANA-CHAMPAIGN/URBANA-DATA/Fiadeiro-Urbana08.pdf>

“For every activity a , a homomorphism $B(a)$ of graphs between the body of $B(a)$ and SF .

(This homomorphism makes configurations *reflective*.)” (ibid., p.9)

“Therefore, we decided to look for algebraic mechanisms of interconnection that can capture **peer-to-peer** interactions among autonomous components. That is why, in this paper, we report on the use of co-spans - pairs $\langle f_A, f_B \rangle$ where $f_A: A \rightarrow S$ and $f_B: B \rightarrow S$ are morphisms of a category D .” (Fiadeiro, CALCO'07, p. 195)

J. L. Fiadeiro, V. Schmitt (2007) Structured co-spans: an algebra of interaction protocols. In T. Mossakowski, U. Montanari, M. Haverlaen (eds) Algebra and Coalgebra in Computer Science. LNCS, vol 4624. Springer, Berlin Heidelberg, pp 194-208

Glue is gravitational, it holds things together by forcing them down.

1.3. Inhaling glue

Along the symbolic interaction metaphor of “I” and “Me” of a “Self”, a duplication of an agent into itself and his inner-environment might open up the possibility for a *reflectional* modeling. Such a reflectional distinction is

reasonable only for a *society* of agents and is of no relevancy for a solipsistic concept of agents. The inhaling concept of reflectional glue is highly solipsistic and is celebrating gluish hedonism. Therefore, to stretch further the antropomorphie metaphor of “I” and “Me” of a “Self” for societal interaction, a new distinction has to be sketched: the distinction between the homogeneity of (empirically) different “Self”s and a heterogeneity between such “Self”s and “Thou”. This move is quickly over-stretching ordinary glue. Between Herbert Mead’s *Self* as I and Me, and Gotthard Gunther’s *Thou* as a fundamentally different “I” and “Me”, a chiasm demands challenging flexibility to any glue:

$$\text{Chiasm} \left(\left(I, Me \right)_{\text{self}} \updownarrow \left(I, Me \right)_{\text{thou}} \right).$$

Such over-stretching is avoided by the denial of a dialogical difference between Self (or I) and Thou.

That is, the functionality of a buffer for sender and receiver could be *incorporated* from the outer-environment (channel) into the inner-environment of an agent as a reflectional part of the sender and receiver interaction. The inner-environment of an agent (Me) is taking the agent-specific elements of glue into its domain. Glue gets inhaled and with this incorporation it is loosing its procrastinating function as a non-computing coordinative buffer. Inhaled glue becomes part of the agent and its computational facilities.

This approach to reflectionality is leading strictly into meta-circular iterations and regresses. Quickly, the incorporated glue is starting to glue itself by incorporating its incorporated glue, endlessly.

A *monocontextural* modeling is drawing a strict distinction between the three identical, i.e. non-reflectional entities:

Sender, Buffer, Receiver with the activities: send, receive, put, get. That is, send-->put, receive<--get.

Therefore, there is no flexibility accessible to model reflectional incorporation of the functionality of buffers into the instances “sender” and “receiver”.

A *polycontextural* modeling is drawing a distinction between two positions and their chiasmic functionality as Sender and as Receiver. Hence, distinctions like “*buffer as receiver*” and “*receiver as buffer*” and also “*buffer as sender*” and “*sender as buffer*” are accessible.

Such a movement towards an *internalization* of the functionality of buffers is reducing the costs of interactions. Because of its chiasmic structure, such an internalization is also free of bad circularity, like the infinite regress of buffering buffers.

Hence, the simple distinction between active and passive processuality of an agent (computation) and buffer (coordination) has to be transformed into an active/passive activity of agents.

2. Getting rid of glue

2.1. Interfaces

2.1.1. Interfaces as mutual representation

Glue-free mediation is still challenging the clue-less approaches of scientific modeling, formalization and implementation of interactivity and interactionality.

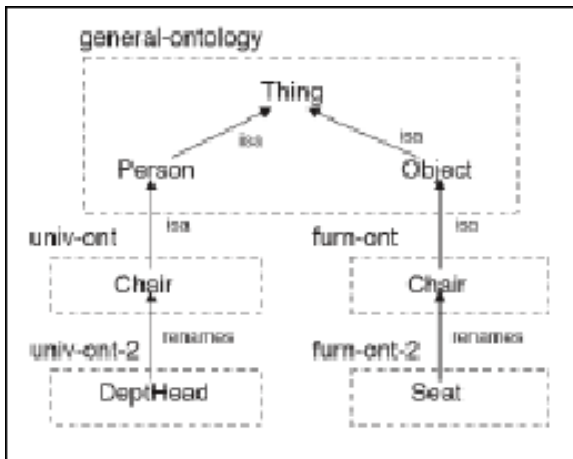
As sketched before, interactions mediated by buffers and their glue are interacting in the ontological-semiotic mode of *is-abstractions* (is-a, has-a) accepting basic presuppositions of identity-driven conceptualization and implementation, i.e. ontology, semiotics and logic.

One of the main problems of modeling in the mode of the is-abstraction is the well known *polysemy* of semantics and its multiple inherence. Despite the amount of academic solutions, the problem remains as long as its identity presupposition, i.e. disambiguation, isn’t changed.

The sold solutions are based on direct or indirect *ad-hoc* principles and *one-step*-thinking.

The example below is base on the ingenuous procedure “*rename*” (Hendle). After renaming the term, the general

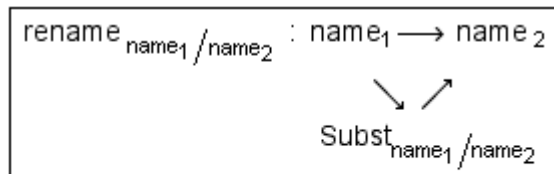
ontology might be prolonged from the general ontology [Thing, Person] with its university-ontology to the furniture-ontology. With this procedure, no conflict will arise. At least as long as nobody starts thinking one step further.



Cost of disambiguation and buffering

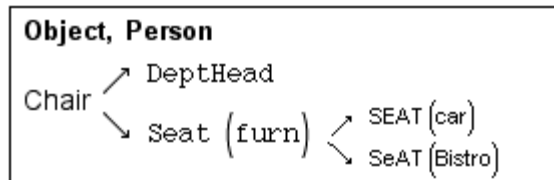
Communication of disambiguated data is cost-free. But it is naive to think that it comes without costs. In contrary, the costs of disambiguation, necessary before any procedures can happen, are enormous. But disambiguation is arbitrarily stopped and is depending on a context. With a change of context, disambiguation has to start again.

Renaming is itself a kind of a buffering, i.e. gluing procedure, lacking any interactivity:

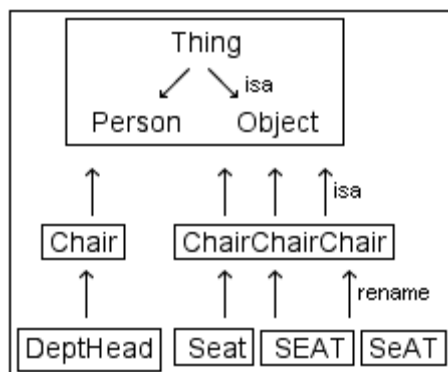


Example

Semantics of *Chair*:



Some renamed and extended ontologies

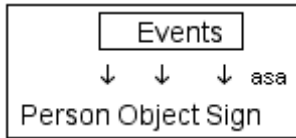


Extensions by renaming are ad-hoc and have to be repeated endlessly through the semantic universe, which is not restricted to the English language only. Even to stop its regress in concrete computing scenarios isn't cost-free. Fixed solutions, glued by chance, have to be re-fixed after the slightest context-change of the fixture. For complex, flexible and mobile computing, simply a disaster.

It is typical for the design of ontologies for semantic purposes in computation, like the Semantic Web, that the medium of its thematization, i.e. language, sign systems, is not mirrored in the General Ontology Language (GOL). GOL is designed in the framework of set theory which is mirroring Aristotelian ontology. There is no place for reflection, self-reflection and interaction between autonomous subjects left.

Reflectional approaches are much involved with the, at least, triadic-trichotomic semiotic in the sense of Peirce (Goguen).

Therefore, to the whatever Aristotelian ontology, at least the “ontology” of the vocabulary “Sign” has to be added for a *conservative* extension of the GOL. Hence, events or phenomena are occurring as Person, Object or Sign in an (semiotically) extended ontology.



Again:
 “No self-reference is possible unless a system acquires a certain degree of freedom. But any system is only free insofar as it is capable of interpreting its environment and choose for the regulation of its own behavior between different interpretations.” Gunther, 1968, p. 44

Hence, glued, i.e. buffered, interaction is unnecessarily cost-intensive even before any computation and coordination can happen.

There are conceptual costs, too. The identity approach, even in a 2-categorical setting, is conceptually restricting possibilities.

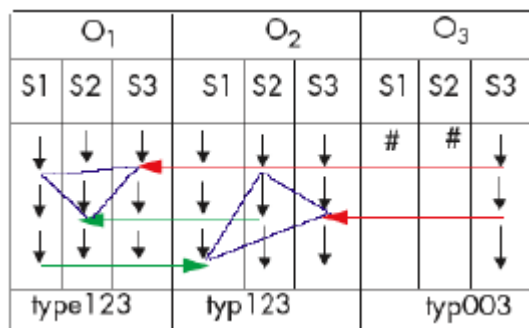
2.1.2. Polycontextural approach

A reflectional analysis of polysemy is an analysis of the semiotic actions of agents which are leading to the phenomenon of polysemy and its possible conflicts with other semiotic or logical principles. Therefore, such an analysis is more complex, because it has to describe the situation intrinsically, that is from the inside and not from the position of an external observer.

The aim of a polycontextural modeling of polysemy is to design the construction of polysemy in a finite and concrete manner.

The distinction of two fundamnetally different kinds of abstractions, the is-abstraction (identification) and the *as-abstraction* (thematization), might help to model the reflectional situation. The formula of the as-abstraction “asa” is: “X as Y is Z”, hence, the is-abstraction “isa”, X is X, can be read as an abbreviation of: “X as X is X”.

The as-abstraction is introducing highest flexibility for modeling, designing and implementing complex *reflectional* situations. The as-abstraction is abstrating from the main principle of any computation and computing: the principle of *identity*.



| PM | O ₁ | O ₂ | O ₃ |
|----------------|----------------------|----------------|----------------|
| M ₁ | chair | □ | □ |
| M ₂ | □ | head | □ |
| M ₃ | chair _{tok} | person | token |

| PM | O ₁ | O ₂ | O ₃ |
|----------------|----------------|----------------|----------------|
| M ₁ | S ₁ | S ₁ | x |
| M ₂ | S ₂ | S ₂ | x |
| M ₃ | S ₃ | S ₃ | S ₃ |

(see below §2.3):

| PM | O ₁ | O ₂ | O ₃ |
|----------------|-------------------|-------------------|-------------------|
| M ₁ | comm ₁ | put ₁ | x |
| M ₂ | put ₂ | comm ₂ | x |
| M ₃ | get ₃ | get ₃ | comm ₃ |

Mono-contextual "isa":

- S1: Chair is part of a furniture ontology (Object),
- S2: Chair is part of a department ontology (Person),
- S3: Chair is part of a vocabulary ontology (Vocabulary).

Poly-contextual "isa as":

- O1S1: Chair as such, that is, as an object (furniture) "Chair", Chair_{obj},
- O2S2: Chair as such, that is, as a person (head) "Chair", Chair_{pers},
- O3S3: Chair as such, that is, as the token (vocabulary) "Chair", Chair_{token}.

| PM | O ₁ | O ₂ | O ₃ |
|----------------|----------------|----------------|----------------|
| M ₁ | S ₁ | x | x |
| M ₂ | x | S ₂ | x |
| M ₃ | x | x | S ₃ |

Here, "as such" means, that the ontologies *Object*, *Person* and *Vocabulary* can be studied and developed for their own, independent of their interactivity to one another but placed and mediated in the constellation of their poly-contextuality, that is, their distribution over the 3 loci, O₁·O₂ and O₃.

Voc O3S3 in Furn O1S3 :

The token "Chair" as used to denote the object "Chair", Chair^{token,obj}

VocO3S3 in Dept O2S3 :

The token "Chair" as used to denote the person "Chair", Chair^{token,Head}

Chair O2S2 in Dept O1S2 :

The object Chair as used in the person ontology Dept, Chair^{obj,Dept}

Chair O1S1 in Furn O2S1 :

The person Chair as used in the object ontology Furn, Chair^{pers,Furn}

| PM | O ₁ | O ₂ | O ₃ |
|----------------|----------------|----------------|----------------|
| M ₁ | S ₁ | S ₁ | x |
| M ₂ | S ₂ | S ₂ | x |
| M ₃ | S ₃ | S ₃ | S ₃ |

Reflectional situations

Chair O2S2 in Dept O1S2:

System O1S1 has in its own domain space for a mirroring of O2S2. This space for placing the mirroring of O2S2 is the reflectional capacity realized by the architectonic differentiation of system O1. In other words, O1 is able to realize the distinction between its own data and the data received by an interacting agent. Data are therefore differentiated by their source, e.g. their functionality, and not only by their content.

| | | | |
|----------------|----------------|----------------|----------------|
| PM | O ₁ | O ₂ | O ₃ |
| M ₁ | S ₁ | x | x |
| M ₂ | S ₂ | S ₂ | x |
| M ₃ | x | x | S ₃ |

Chair O1S1, in Furn O2S1:

System O2S1 has in its own domain space for a mirroring of O1S1.

| | | | |
|----------------|----------------|----------------|----------------|
| PM | O ₁ | O ₂ | O ₃ |
| M ₁ | S ₁ | S ₁ | x |
| M ₂ | x | S ₂ | x |
| M ₃ | x | x | S ₃ |

A (re)solution of the problem

The department Dept for itself has no conflict with polysemy. This conflict between Dept and Furn is mediated by the Voc. That is, the Person of the Dept as Chair is a person and nothing else.

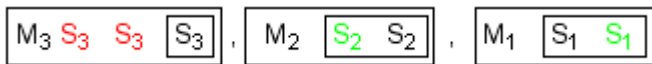
The furniture Furn for itself has no conflict with polysemy. This conflict between Furn and Dept is mediated by the Voc. That is, the Chairs as objects of the Furn are chairs and nothing else.

The vocabulary Voc for itself, containing "Chair", has no conflict with the polysemy between Dept "Chair" and Furn "Chair".

The *meaning* of the polysemic situation is realised by

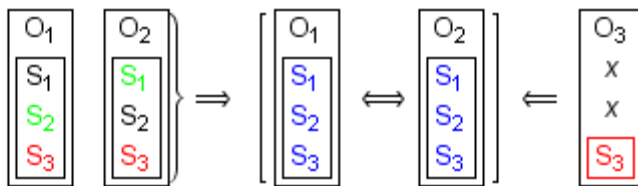
Meaning of (O3S3) = interaction of (O1S3, O2S3)

| | | | |
|----------------|----------------|----------------|----------------|
| PM | O ₁ | O ₂ | O ₃ |
| M ₁ | S ₁ | S ₁ | x |
| M ₂ | S ₂ | S ₂ | x |
| M ₃ | S ₃ | S ₃ | S ₃ |



The conditions for a conflict arises exactly between

O1 (S1,2,3) and O2 (S1,2,3) mediated by O3S3 as visualized by the blue triangles.



Both Furn and Dept are using Voc and both are using the string Chair of Voc. Both are different and are mapping the Voc differently relative to their position, thus the Voc has to be distributed over different places according to its use or functionality. The Voc used by Furn is in another functionality than the Voc used by Dept.

Up to now we have not yet produced a contradiction but only a description of the situation of *polysemy*, that is, the necessary conditions for a possible ontological, semantic and logical contradiction.

A user-oriented approach to the modelling of polysemy has to ask "*For whom is there a conflict?*" Therefore, we have additionally to the semantic and syntactic modelling of the situation to introduce some pragmatic instances. In our example this could be the user of a *Query* which is answering in a contradictory manner.

Query's contradictory answer

Now we have to deal with the contextures: (Query, Voc, Furn, Dept).

In the classic situation, the Query answers with a logical conjunction of Chair as Person *and* Chair as a Department member, which both are logico-semantically excluding each other and therefore producing for the user

of the Query a conflicting or contradictory answer if put into a single logical conjunction.

Logic comes into the play also for the polycontextural modelling, but here *conjunctions* too, are distributed over different contextures. And therefore, a contradiction occurs only if we map the complex situation all together onto a single contexture.

(O₄M₄) = Query

| PM | O ₁ | O ₂ | O ₃ | O ₄ |
|----------------|----------------|----------------|----------------|----------------|
| M ₁ | S ₁ | S ₁ | x | □ |
| M ₂ | S ₂ | S ₂ | x | □ |
| M ₃ | S ₃ | S ₃ | S ₃ | □ |
| M ₄ | □ | □ | □ | S ₄ |

Logic:

$$\text{Person} \cap \text{Object} \cap \text{Vocabulary} = \emptyset,$$

$$\text{Person}(\text{Chair}) \equiv \neg \text{Furniture}(\text{Chair}) \equiv \neg \text{Vocabulary}(\text{Chair})$$

$$\text{Chair} \in \text{Department} \implies (\text{Chair} \notin \text{Furniture} \wedge \text{Chair} \notin \text{Vocabulary})$$

Contradictory Answer:

$$(\text{Chair} \in \text{Department} \wedge \text{Chair} \in \text{Furniture}) \implies (\text{Chair} \in \text{Department} \wedge \text{Chair} \notin \text{Department}) : \#$$

Polylogic

$$\text{Chair} \in (\text{Department}, \text{Furniture}, \text{Vocabulary})$$

$$\text{Person} \cap \text{Department} = \emptyset, \text{Person} \equiv \neg \text{Department}$$

$$\left[\begin{array}{l} \text{Chair} \in^1 \text{Department}, \text{Chair} \notin^1 \text{Furniture}, \text{Chair} \notin^1 \text{Vocabulary} \\ \text{Chair} \in^2 \text{Furniture}, \text{Chair} \notin^2 \text{Department}, \text{Chair} \notin^2 \text{Vocabulary} \\ \text{Chair} \in^3 \text{Vocabulary}, \text{Chair} \notin^3 \text{Department}, \text{Chair} \notin^3 \text{Furniture} \end{array} \right]$$

$$\text{Polylogic with Conjunctions: } \wedge^{(3)} \equiv (\wedge^1 \wedge^2 \wedge^3),$$

$$\text{Negations: } \neg^i, i = 1, 2, 3 \text{ and non-entailments: } \neg^i \in \equiv \notin^i$$

$$(\text{Chair} \in^1 \text{Department} \wedge^{(3)} \text{Chair} \in^2 \text{Furniture}) \implies (\text{Chair} \in^1 \text{Department} \wedge^{(3)} \text{Chair} \notin^2 \text{Department})$$

$$\left(\begin{array}{l} \text{Chair} \in^1 \text{Department} \wedge \text{Chair} \notin^1 \text{Department} \implies \emptyset \\ \text{Chair} \in^2 \text{Furniture} \wedge \text{Chair} \notin^2 \text{Furniture} \implies \emptyset \\ \text{Chair} \in^3 \text{Vocabulary}, \text{Chair} \notin^3 \text{Vocabulary} \implies \emptyset \end{array} \right)$$

$$\left(\begin{array}{l} \text{Chair} \in^1 \text{Department} \wedge^1 \text{xxx} \\ \text{xxx} \wedge^2 \text{Chair} \notin^2 \text{Department} \\ \wedge^3 \text{Chair} \in^3 \text{Vocabular} \end{array} \right) \implies^{(3)} \left(\begin{array}{l} \text{Chair} \in^1 \text{Department} \wedge^1 \text{xxx} \\ \text{xxx} \wedge^2 \text{Chair} \in^2 \text{Furniture} \\ \wedge^3 \text{Chair} \in^3 \text{Vocabular} \end{array} \right)$$

$$\text{Short: } (\text{Chair} \in^1 \text{Department} \wedge^{(3)} \text{Chair} \in^2 \text{Furniture} \wedge^{(3)} \text{Chair} \in^3 \text{Vocabulary}).$$

If we give up all the introduced ontological distinctions of polycontexturality and reducing therefore our ontologies to a single mono-contextural general ontology we saved our famous contradiction again. But now, this

contradiction is a product of a well established mechanism of reduction. And sometimes it isn't wrong to have it at our disposition.

The costs of the polycontextural approach lies in its novelty and its intrinsic complexity.

Observations about observations in another worldmodel

"Unlike observation of the first order, which sees all elements in the world as connected in one context with geometric symmetry, observation of the second order views a world that is poly-contextual (polykontextural). In the poly-contextual world, the values of social institutions may not all be in the same context. From such perspective, labeling two values in different contexts as a set of binary for comparison in the same matrix is deemed to generate inaccurate analysis.

This is why "many-valued-logic" (mehrwertige Logik) is so essential in the poly-contextual world. When the values in seemingly antithetical binaries are, in fact, of different contexts, for those values to be antithetical yet mutually complementary is no longer impossible. In fact, this antithetical yet complementary pattern that is unthinkable in the realm of the world of the observation of the first order is totally consistent with the many-valued-logic of poly-contextual settings.

According to Lin, this many-valued-logic is exactly the essence of traditional Chinese law and its legal system." Review: Duan Lin. _Weibo Lun Zhongguo Chuantong Falu_(Weber's Analysis on Chinese Traditional Law: Critiques on Weber's Comparative Sociology)

Dr. Lin Duan has provided a profound study on the demerits of Weber's methodology. See Lin Duan, Rujia lunli yu falü wenhua: shehuixue guandian de tansuo (Confucian Ethics and Legal Culture: Exploration from Sociology), Beijing: Zhongguo zhengfa daxue, 2002, p. 93; 122.

2.2. Diamond modeling

2.2.1. General strategies

Diamond constructions are reducing the costs of interactivity by the fact that their operations are intrinsically interactive. That is, the interplay of the conditions of matching and the compositions themselves are reflected in the complementarity of categories and saltatories of diamonds.

Diamonds are offering more structural space to model and implement interactivity than categories and n-categories.

The general strategy to reduce the costs of interaction is to find a concept and apparatus that is offering a wider *logical scope* to model the dynamics of the differences between actors and their communication.

The other part of the strategy is to *separate* basic functions, like coordination/computation (Fiadeiro) or locality/connectivity (Milner). Both strategies are changing the priority of time in computing to the favor of space, "*metaphorical space*" (Milner) for the localization of separated aspects of (mobile) computation.

This enlargement of "*metaphorical space*" happens for computer science in different steps, all trying to capitalize on new and broader concepts from other disciplines or on developing own computer science specific concepts, like , e.g. Goguen's Institutions and Padawitz' Swinging Types.

Modal logics

Coalgebra

Category theory

Combining logics

n-Category theory

But there are some fundamental limitations occurring in this endeavour.

"Grammatologically, the Western notational system is not offering space in itself to place sameness and otherness necessary to realize interaction/ality. Alphabetism is not prepared to challenge the dynamics of interaction directly. The Chinese writing system in its scriptural structuration, is able to place complex differences into itself, necessary for the development and design of formal systems and programming languages of interaction. The challenge of interactionality to Western thinking, modeling and design interactivity has to be confronted with the

decline of the scientific power of alpha-numeric notational systems as media of living in a complex world.
“ (Interactivity, 2008)

To overcome such limitations, the graphematic and trans-classical strategies of:

Polycontextuality,

Morpho- and Kenogrammatics,

Proemiality and Chiasm,

Diamond theory,

had been introduced as subversive and experimental interventions and realized in form of fragmentarism.

It seems that for each step there is a progressive extension of the possibilities of ‘space-ing’ interactionality and reflectionality of notational systems.

All known strategies have their own advantages and deficits. The main problems are not so much the limitations of the specific approaches but their applications to domains for which they are not specifically designed and are therefore inadequate albeit the compaigning propaganda.

It surely would be an absurd misunderstanding, also quite typical for the ‘quick-reading’ ritual of censors, to believe that I am hallucinating a computer science based on Ancient Chinese hieroglyphs. (Kaehr, The Chinese Challenge).

2.2.2. Categorical composition

"Category Theory is advocated as a good mathematical structure for this integration precisely because it focuses on relationships and interactions! The focus that Category Theory puts on morphisms, as structure preserving mappings, is paramount for Software Architectures because it is the morphisms that determine the nature of the interconnections that can be established between objects (system components)." (Fiadeiro, 2002, p. 12)

Category oriented implementations are based on the concept of categorical *composition* of morphisms which in itself is neither interactive nor reflective. It is mentioned that morphisms are representing interactions and interconnections. This might be appropriate for non-reflectional interactions, like actions on objects (Bunge). Reflection, and especially social reflection, gets into conceptual trouble. Interaction might be represented by morphisms, but reflection would then be represented by ‘morphisms of morphisms’.

This figure leads automatically to the question: Is a morphism of a morphism, i.e. a second-order morphism (cf. Fiadeiro’s homomorphism!) conceptually a morphism or something else? If it is conceived as a morphism, we are back again to the first-order concept of morphisms, i.e. to morphisms without reflection. And hence, the second-order concept can be reduced to a first-order concept. Otherwise, if the construct of a morphism of a morphism isn’t reducible to a first-order categorical concept, then it is violating the axioms of the framework of category theory, especially its axiom of identity.

Hence, the workspace of the categorical interpretation of interactivity is modeled by the metaphors of super glue, for categories, and of stretched glue, for n-categories.

Such *societal* and *reflectional* metaphors are reasonable for computer science only if they are explicitly declared as *weak* metaphors, not suitable for social and psychological adaption. Albeit the fact that interdisciplinary *confusions* are supporting academic marketing strategies, they are nevertheless boring and economically and politically dangerous.

2.2.3. Dissemination

The dissemination of categorical systems in the sense of polycontextuality is offering the possibility of interactionality and reflectionality. But still for a considerable price of interpretative, i.e. observer depending, delays. Interactivity between disseminated contextural systems is guided by the strategies and mechanism of proemiality and are realized as chiasm.

Each contexture of a contextural compound constellation is composed by sub-contextures, usually as elementary

morphisms and is of trichotomic structure. Thus, polycontextuality is a dissemination of trichotomic structures, that are, in themselves, not prepared to reflect their interactionality. Interactionality and reflectionality are introduced polycontexturally as interactions between different contextures, i.e. as trans-contextural events.

2.2.4. Chiasm

From an observer theoretical point of view, chiasms between contextures, realizing interactivity, is observed from an external observer. Hence, their internal mechanism is still not yet glue-free, but involved in a kind of a dissolution of the adhesion of glue, i.e. the chiastic jump between disseminated contextures is still sniffing glue and sticking the elements of mediation together by some metaphysical or kenomic glue.

Chiastic glue is technically delivered mainly by the *coincidence* relations of chiasms. They are responsible for guaranteeing that the distributed order relations, which are themselves glued by definition (matching conditions), and their risky exchange relations interact in harmony with similitude. The fulfillment of the coincidence relations in a chiasm is establishing categorial similarity, i.e. family resemblance of categorial kind. Otherwise, chiastic glue would be over-stretched and loosing its ends.

In other words, for chiasms to work, their relationality has to be in categorial harmony of similitude. Chiastic concepts have to fit together by general mappings or morphisms. Chiastic jumps, possible in chiasms, are insured by harmony and traced back and ruled by the coincidence or similarity relations. This important restriction and complicity to similarity is necessary for chiasms to avoid empty statements, like “*everything is connected*”, of universal connectionism. It also prevents jumps into the void.

Super-glue and stretched super-glue interactions, realized as buffers and buffered systems, don't need observers. They are designed and conceived as observer-independent objective utilities and mechanisms.

Therefore, the observer-independent approaches might be adequate for *signal* and *information* processing (information interaction) but are missing the demands for interactional situations of *semantic* and *knowledge* modeling and computation (symbolic interaction).

2.2.5. Diamondization

Jumps without guaranteed security have to be realized by somersaults, i.e. by salti. Salti are in a strict discontextural opposition to glued connections and secured journeys involving jumps. Hence, their theoretical modeling happens with the saltisations of saltatories. Saltatories are building together with categories diamonds. What has to be risked is to stage-manage the drama of glue-free interactions and reflections within the framework of diamond theory. But metaphors like “*stage*” and “*framework*” are misleading by their unbroken coherence.

Categories: duality

Chiasms: guided complementarity or family resemblance (Wittgenstein)

Diamonds: discontextural complementarity

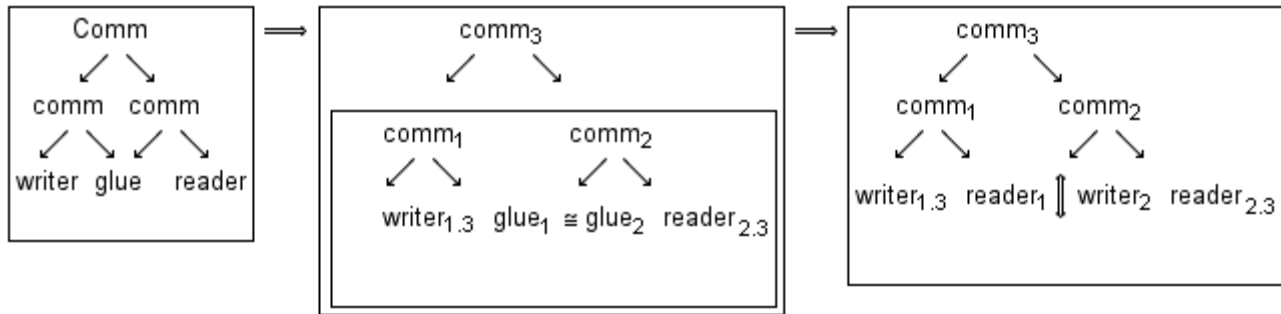
The epistemic tendencies “computation” and “coordination” (Fiadeiro) are thematized by the diamond strategies as complementary, antidromic and parallax.

Diamonds are offering a new kind of a “metaphoric space” to distribute both tendencies while keeping their autonomy untouched. With such a heterarchic order between computation and coordination there is no need to suppress the computational aspects of coordination and the coordinational aspects of computation.

This is in contrast to the n-categorical modeling where there is no concept and no mechanism available on a principle level to implement the antagonistic epistemical directions of computation and coordination. Furthermore, both are set by the categorial approach into a *hierarchical* order: first computation, then coordination or the other way round: first coordination, then computation. Both are strictly excluding “*social life*”, i.e. interaction between computation and coordination.

2.3. Sketch of formal chiasitic and diamond modeling

From hierarchy to heterarchy



Matrix modeling

| PM | O ₁ | O ₂ | O ₃ |
|----------------|---------------------|---------------------|-------------------|
| M ₁ | comm ₁ → | write ₁ | x |
| M ₂ | write ₂ | ← comm ₂ | x |
| M ₃ | read ₃ → | read ₃ → | comm ₃ |

| PM | O ₁ | O ₂ | O ₃ |
|----------------|-----------------------|-----------------------|-----------------------|
| M ₁ | sender ₁ → | write ₁ | x |
| M ₂ | write ₂ | ← sender ₂ | x |
| M ₃ | read ₃ → | read ₃ → | receiver ₃ |

| PM | O ₁ | O ₂ | O ₃ |
|----------------|-------------------|-------------------|-------------------|
| M ₁ | comm ₁ | put ₁ | x |
| M ₂ | put ₂ | comm ₂ | x |
| M ₃ | get ₃ | get ₃ | comm ₃ |

Communication (Sender, Receiver)

comm₁ as sender₁ = put₁ to O₂ @ O₂ M₁

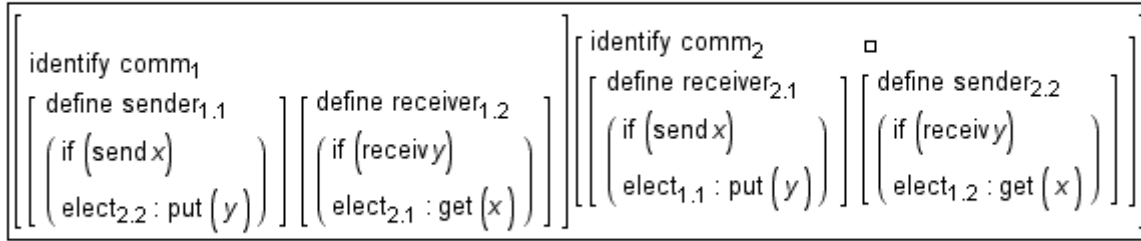
comm₂ as sender₂ = put₂ to O₁ @ O₁ M₂

comm₃ as (receiver₁ • receiver₂) = get₃ from O₁ M₂, get₃ from O₂ M₁.

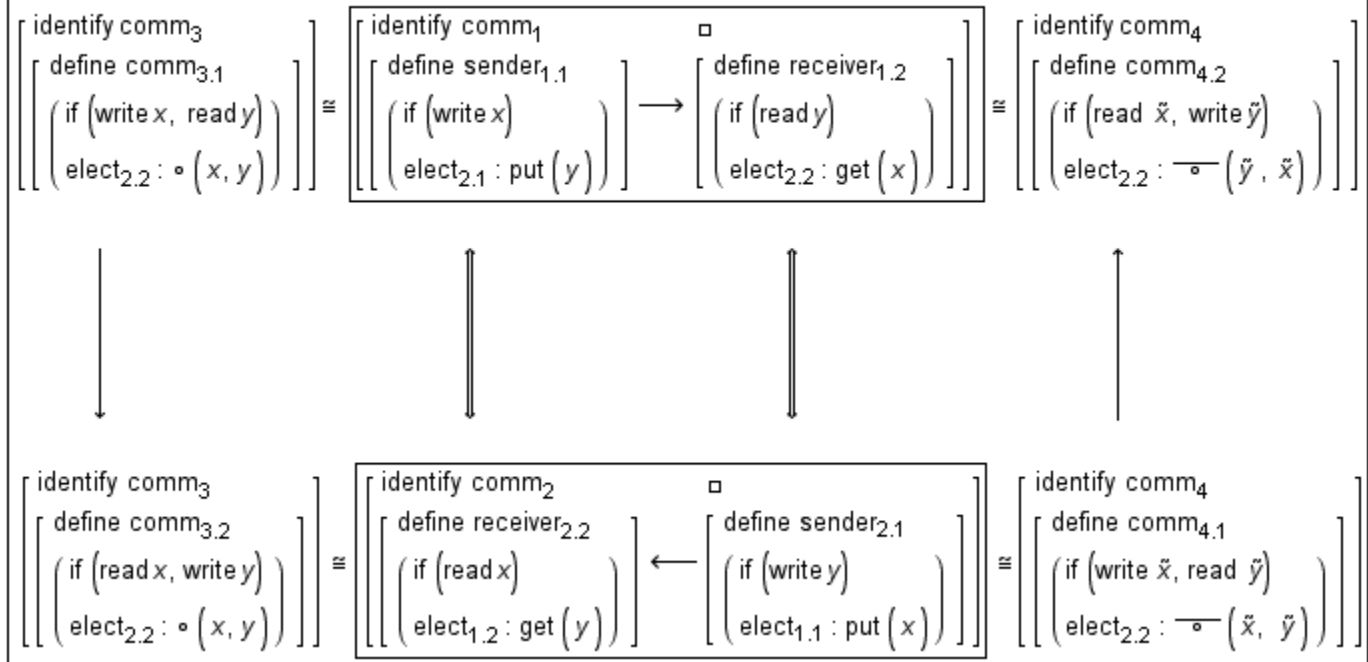
Contextual modeling in ConTeXtures

| | | |
|---------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| style interactional | | |
| topics symbolic ;; < comm _i : symb _i —> symb _i , i = 1, 2, 3 > | | |
| thematize Comm ⁽³⁾ ;; < scenario: Comm ⁽³⁾ = (comm ₁ , comm ₂ , comm ₃) | | |
| identify comm ₁ define sender ₁ (lambda (x) (if (send x) (put (y)))) (elect ₂) | identify comm ₂ define receiver ₂ (lambda (y) (if (receiv y) (get (x)))) (elect ₃) | identify comm ₃ define comm(sender ₁ / receiver ₂) (lambda (x, y) (lambda (comm) (if (put x) (get y) (comm ₃ : sender ₁ receiver ₂)))) (elect ₁ elect ₂) |

Matrix modeling in ConTeXtures of chiasm (send, receive, pos)



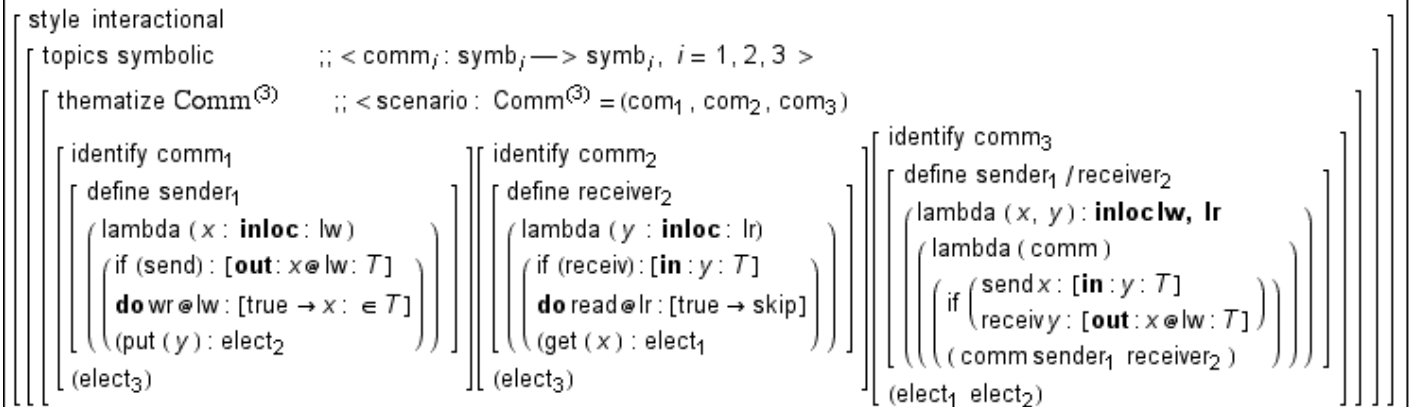
Basic Diamond modeling of interactional Communication



Recursivity of communication

Communication, modeled as a chiasm is not only structural but also procedural construction. Its recursivity is not intr contextural but distributed over different conxtures, hence trans – contextural.

Chiastic modeling of communication in ConTeXtures by mimicking Fiadeiro 's specifications



2.4. Costs and resources

2.4.1. Conceptual analysis

There are many ways to measure costs, efficiency and resources of computational interaction and communication. One quite direct way might be to show the parallel, or heterarchical structure of diamond modeling and implementation in contrast to hierarchical understanding of interaction and communication. With the presumption that “parallel” processing is more cost-efficient than non-parallel computing. And obviously, it has to be shown that polycontextural and diamond computation is at least conceptually “parallel”.

Hence, using glue to organize hierarchically interaction, or even: the ‘*social life*’ of computing is, from the very beginning, more expensive and less efficient than heterarchical polycontextural and diamond computing.

Such considerations about efficiency and cost can be analyzed in detail for specific constellation.

Structural costs of deepness and broadness of a formula are not to be confused with the well-known complexity analyses based on computational time of big Omikron: $O(n)$.

An analysis of the *system structures* of glued interaction and of chiasmic and diamond interaction can be put into the simple results:

The kernel of *glue*-modeling consist of 3 unique instances (ports) at 1 locus (or nil), e.g. $\text{Comm} = (\text{sender}_0, \text{glue}_0, \text{receiver}_0)$.

The kernel of *chiasmic* modeling consist of 2 unique instances (roles) at 3 loci, e.g. $\text{Comm}^{(3)} = (\text{sender}_i, \text{receiver}_i), i=1,2,3$.

The kernel of *diamond* modeling consist of 2 unique instances (roles) at 4 loci, e.g. $\text{DiamComm}^{(4)} = (\text{sender}_i, \text{receiver}_i), i=1,2,3,4$.

The main difference between glued and mediated communication, i.e. between “ $\text{Comm} = (\text{sender}_0, \text{glue}_0, \text{receiver}_0)$ ” and “ $\text{Comm}^{(3)} = (\text{sender}_i, \text{receiver}_i), i=1,2,3$ ” and its mediation operation, is the fact that “*glue*” is a (coordinative) *instance* (object) for “ $(\text{sender}_0, \text{receiver}_0)$ ” while “*mediation*” is a (computational) *process* (action) between the positions $\text{pos}_i, i = 1, 2, 3$ of “ $\text{sender}_i, \text{receiver}_i$ ”.

Structural Costs

$\text{cost}(X) = (n, m)$

n: deepness

m: broadness

$\text{cost}(\text{glue}) = (3, 1)$,

$\text{cost}(\text{chiasm}) = (2, 3)$,

$\text{cost}(\text{diamond}) = (2, 4)$

In other terms, deepness is representing computational complexity and broadness corresponds to the degree of polycontextural coordination and organization of disseminated computations.

2.4.2. Concept tree analysis

Concept and Kantarovic tree analyses for polycontextural constellations (formulas, etc.) can serve as a measure for structural complexity by the degree of *deepness* and *broadness* of the fundamental constructs of a situation.

Broadness is the measure of the degree of dissemination, deepness is the conventional measure of the complexity of a formula. Because of their monocontextuality, broadness is set to 1 for all classical formalizations.

Speed vs. directness

Speed of computation is crucial for closed non-interactive computational systems, i.e. for algorithmic computation. For interactive systems *directness* of reaction to change of the system/environment relationship are crucial. It is clueless to finish in high speed a calculation which has become obsolete in its premises because the situation has changed. The measure for interactive systems is directness of response and not speed of calculation. From the point-view of the calculation paradigm, higher directness appears as higher speed. But that’s misleading. Directness means less steps to calculate and not higher speed.

Optimization for interactive computing systems means optimizing the architectural organization to support

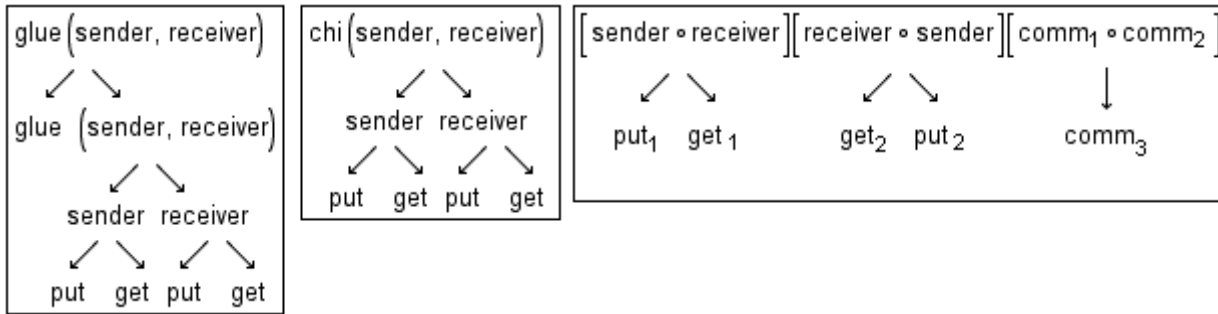
directness.

Speed for algorithmic systems is connected with computational time, i.e. with temporalization. Directness of interactional systems is connected with organizational space, i.e. with architectonics and topology. Organization (coordination) and computation are complementary as are directness and speed.

hierarchic

chiastic

heterarchic modeling



Optimization for interactional computing systems means optimizing the architectural organization to support directness.

Speed for algorithmic systems is connected with computational time, i.e. with temporalization. Directness of interactional systems is connected with organizational space, i.e. with architectonics and topology. Organization (coordination) and computation are complementary as are directness and speed.